



Simulation of Rigid and Flexible Multibody Systems

Tutorial at the Modelica'2008 Conference

Bielefeld, March 3rd, 2008

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Institute of Robotics and Mechatronics







On the provided Software and Documents

- be sure to have Dymola Modelica 2008 installed
- copy folder **FlexibleBodiesLib 1.1 Modelica2008** to your harddrive
 - contains FlexibleBodiesLib 1.1 with specific license
 - subpackage Tutorial with tutorial examples
- copy/open **MultibodyTutorialModelica2008.pdf**



Contents

- Modelica Multibody Basics 
- Modelica Multibody Advanced 
- Exercise 1: Control of an inverse pendulum
- Exercise 2: Hexapod
- FlexibleBodies Library: Beams 
- Exercise 3: Aircraft Fin
- FlexibleBodies Library: General bodies based on finite element data 
- Exercise 4: Rod

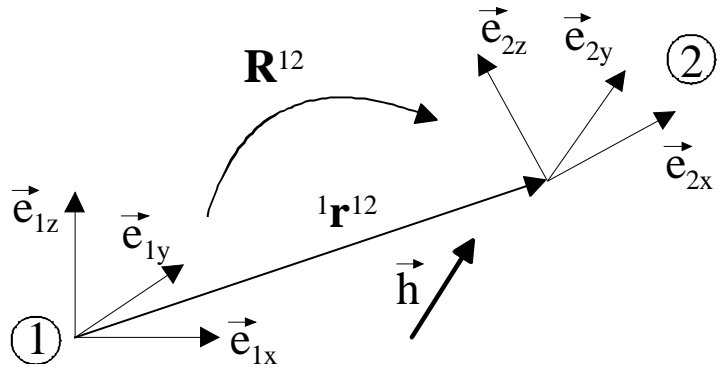
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Modelica Multibody Basics: Orientation

➤ Coordinate systems and their orientation



```
import MultiBody.Frames;
Frames.Orientation R12;
Real h1[3] "h resolved in frame 1";
Real h2[3] "h resolved in frame 2";
equation
  h2 = Frames.resolve2(R12, h1); //or
  h1 = Frames.resolve1(R12, h2);
```

➤ Orientation object R^{12}

➤ describes orientation of coordinate system 2 wrt. 1

➤ holds

```
Real T[3, 3] "Transformation matrix from world frame to local frame";
SI.AngularVelocity w[3]
  "Absolute angular velocity of local frame, resolved in local frame";
```

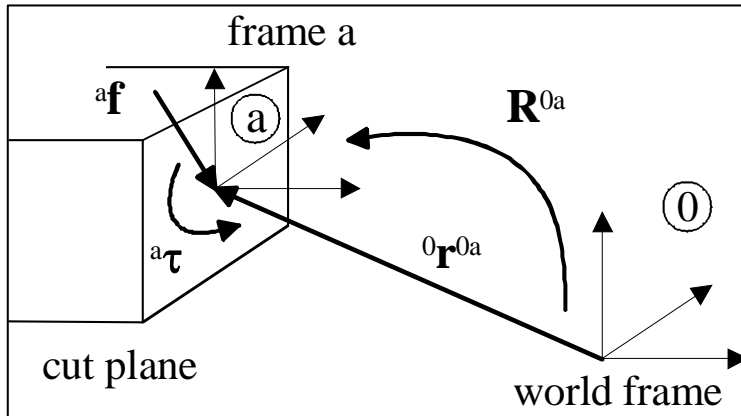
➤ may be computed using rotation angles or quaternions

➤ Multibody Lib. contains over 30 functions to operate on orientation objects

- Frames
- Orientation
- orientationConstraint
- angularVelocity1
- angularVelocity2
- resolve1
- resolve2
- resolveRelative
- resolveDyade1
- resolveDyade2
- nullRotation
- inverseRotation
- relativeRotation
- absoluteRotation
- planarRotation
- planarRotationAngle
- axisRotation
- axesRotations
- axesRotationsAngles
- smallRotation
- from_nxy
- from_nxz
- from_T
- from_T2
- from_T_inv
- from_Q
- to_T
- to_T_inv
- to_Q
- to_vector
- to_exy
- length
- normalize
- axis

Modelica Multibody Basics: Connectors I

- Connectors: the interface to connect components
 - Position is resolved in world frame
 - Forces and torques are resolved in local frame



```
connector Frame
  "Coordinate system fixed to the component with one cut-force and cut-torque (no icon)"
  import SI = Modelica.SIunits;
  SI.Position r_0[3]
    "Position vector from world frame to the connector frame origin, resolved in world frame";
  Frames.Orientation R
    "Orientation object to rotate the world frame into the connector frame";
  flow SI.Force f[3] "Cut-force resolved in connector frame" a;
  flow SI.Torque t[3] "Cut-torque resolved in connector frame";
end Frame;
```

non-flow !

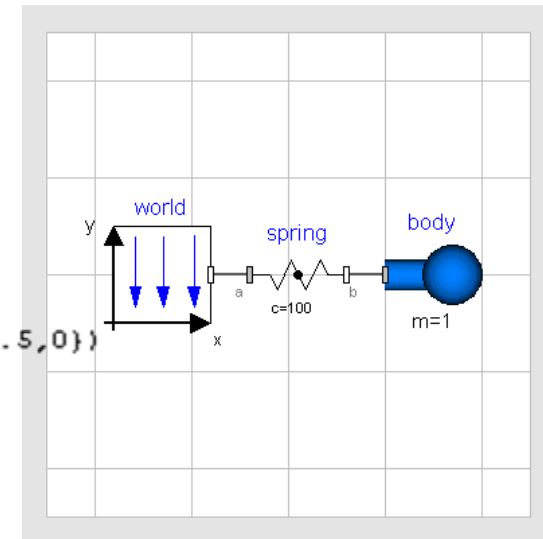
flow !



Modelica Multibody Basics: Connectors II

➤ Connectors: how they work

```
model SpringMass
  inner Modelica.Mechanics.MultiBody.World world
    a;
  Modelica.Mechanics.MultiBody.Forces.Spring spring(c=100)
    a;
  Modelica.Mechanics.MultiBody.Parts.Body body(x_0_start={0,.5,0})
    a;
equation
  connect(world.frame_b, spring.frame_a) a;
  connect(spring.frame_b, body.frame_a) a;
end SpringMass;
```



➤ Modelica's general connections rules

- non-flow variables are set to be equal, i.e. frames coincide
 - since they represent „some kind of potential“
- flow variables sum to zero (Kirchhoff's current law)
 - since they represent time derivatives of preserved quantities
 - are consequently set to zero if connector is not connected to anything

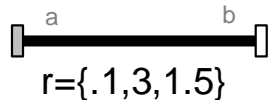
➤ see Modelica.UsersGuide.Connectors for a comparison of connectors in various domains

Modelica Multibody Basics: Components I

➤ Kinematics:

- Component equations provide relations between connector variables on position level
- MultiBody.Parts.FixedTranslation
i.e. fixed translation of frame_b with respect to frame_a
- Tool (e.g. Dymola) differentiates these equations twice for dynamics

fixedTranslation

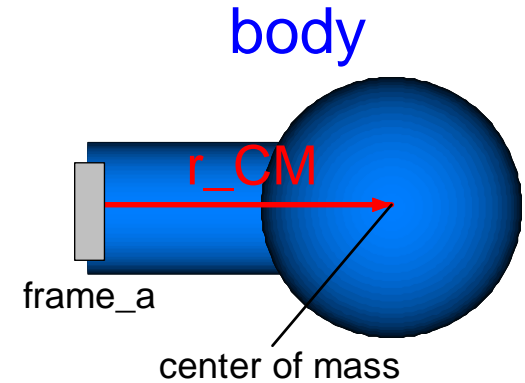


```
frame_b.r_0 = frame_a.r_0 + Frames.resolve1(frame_a.R, r);  
frame_b.R = frame_a.R;  
  
/* Force and torque balance */  
zeros(3) = frame_a.f + frame_b.f;  
zeros(3) = frame_a.t + frame_b.t + cross(r, frame_b.f);
```

Modelica Multibody Basics: Components II

➤ Dynamics

- Newton-Euler equations
- MultiBody.Parts.Body

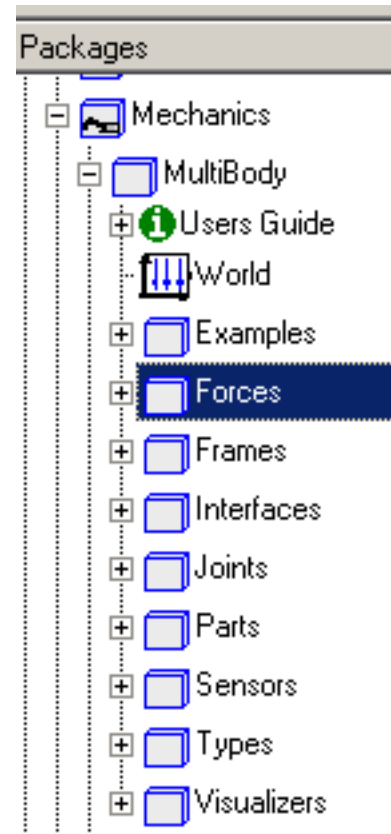


```
// import Modelica.Mechanics.MultiBody.Frames;
// translational kinematic differential equations resolved in local frame_a
v_a = Frames.resolve2(frame_a.R, der(frame_a.r_0));
a_a = der(v_a);

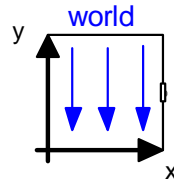
// rotational kinematic differential equations
w_a = Modelica.Mechanics.MultiBody.Frames.angularVelocity2(frame_a.R);
z_a = der(w_a);

// Newton/Euler equations with respect to center of mass
a_CM = a_a + cross(z_a, r_CM) + cross(w_a, cross(w_a, r_CM));
f_CM = m*a_CM;
t_CM = I*z_a + cross(w_a, I*w_a);
frame_a.f = f_CM;
frame_a.t = t_CM + cross(r_CM, f_CM);
```

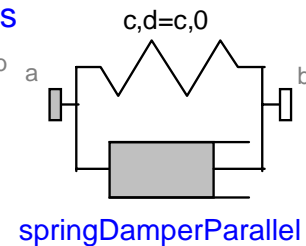
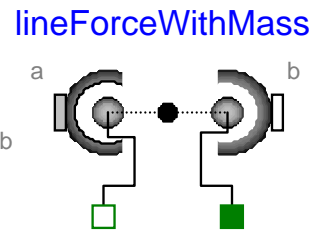
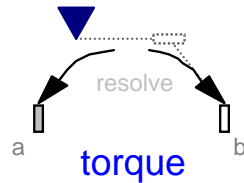
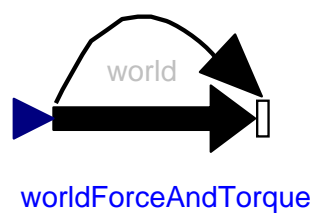
Modelica Multibody Basics: Elementary Components I



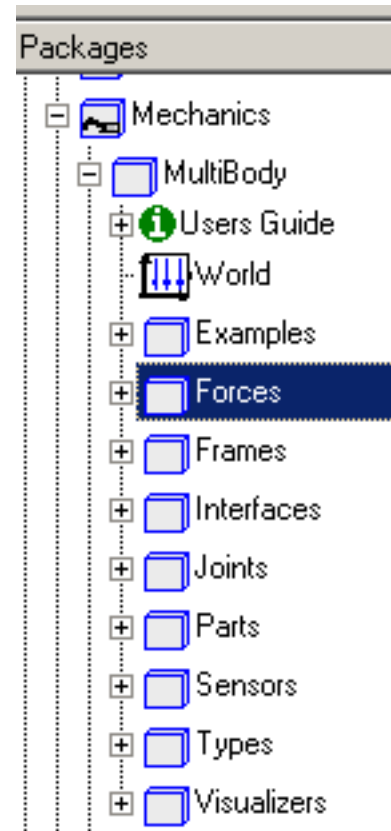
- Modelica.Mechanics.MultiBody.World
 - defines inertial frame, gravity, animation defaults



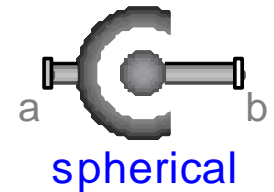
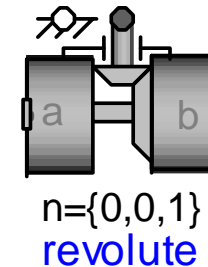
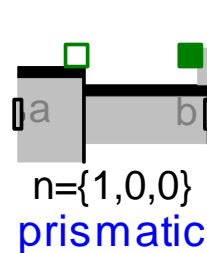
- Modelica.Mechanics.MultiBody.Forces
 - different resolution properties
 - interface to Real input functions and 1D mechanics
 - several spring/damper configurations



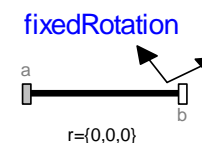
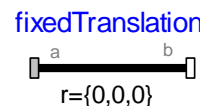
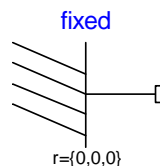
Modelica Multibody Basics: Elementary Components II



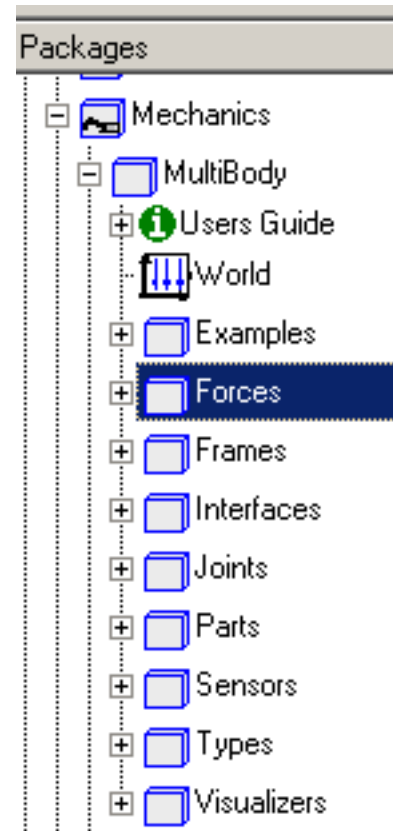
- Modelica.Mechanics.MultiBody.Joints
 - define specific degree of freedom
 - capability to set-up initial configuration
 - interface to/for 1D mechanics and rheonom motion
 - e.g.:



- Modelica.Mechanics.MultiBody.Parts
 - Fixed, FixedTranslation and FixedRotation

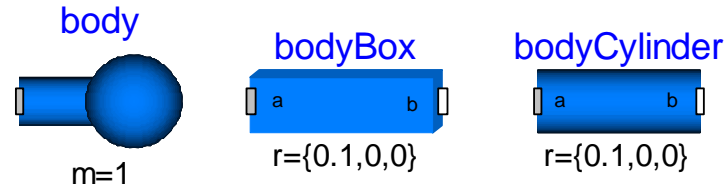


Modelica Multibody Basics: Elementary Components III



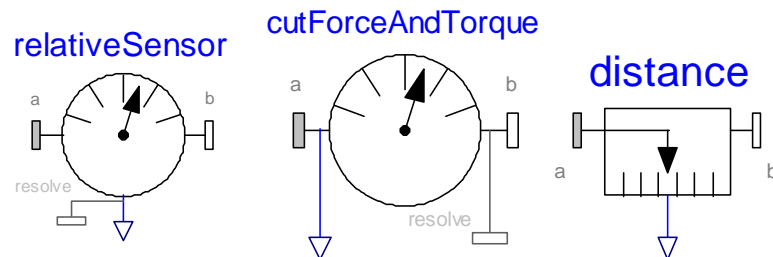
➤ Modelica.Mechanics.MultiBody.Parts

- Rigid bodies with predefined geometric shapes

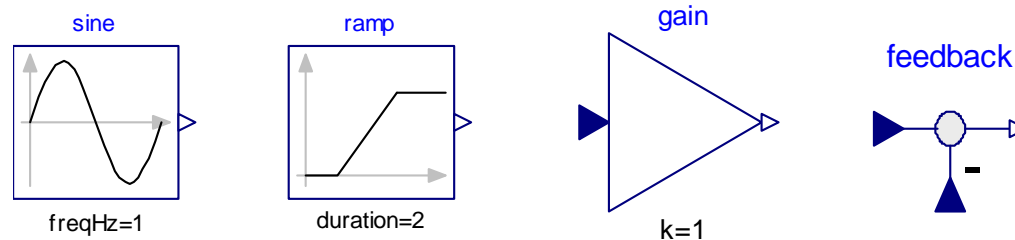


➤ Modelica.Mechanics.Multibody.Sensors

- for control and validation purposes



➤ Modelica.Blocks.Sources + Modelica.Blocks.Math



Modelica Multibody Basics: Analysis Methods

- Model check
- Experiment setup, translation and time simulation

The screenshot displays the Modelica IDE interface for the 'InversePendulum' model. The top window, titled 'InversePendulum - Tutorial.exercises.InversePendulum - [Diagram]', shows the model's structure in the 'Packages' pane and a toolbar with a red circle highlighting the 'Check' icon. The 'Messages - Dymola' window below it reports a successful check: 'Check of Tutorial.exercises.InversePendulum: DAE having 1836 scalar unknowns and 1836 scalar equations. Check of Tutorial.exercises.InversePendulum successful.'

The middle window, titled 'InversePendulum - Tutorial.exercises.InversePendulum', shows the simulation controls. The toolbar has two red circles highlighting the 'Run' and 'Stop' icons. The 'Experiment Setup' dialog is open, showing the following configuration:

- Experiment Name: InversePendulum
- Simulation interval: Start time 0, Stop time 5
- Output interval: Interval length 0, Number of intervals 500
- Integration: Algorithm Dasl, Tolerance 0.0001, Fixed Integrator Step 0

The bottom window shows the 'Variables' pane with a tree view of the model's components: InversePendulum_StateControl 1, InversePendulum 2, world, bodyBox, bodyCylinder, fixedTranslation, actuatedRevolute, and prismatic. The 'Advanced' button is visible at the bottom.

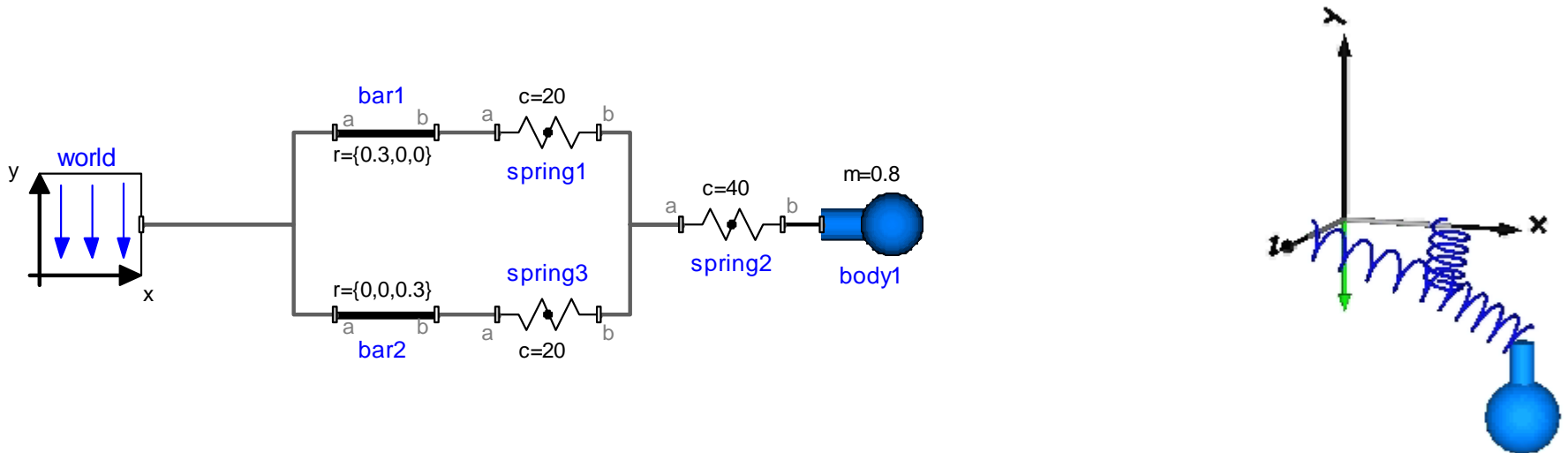
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Modelica Multibody Advanced: State selection I

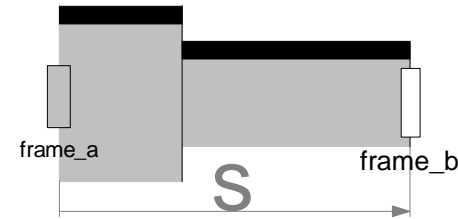
- Joints AND bodies have potential states
 - number of joints is independent from number of bodies
 - an assignment of joints to bodies is not mandatory
 - force elements may be connected to each other
 - e.g.:



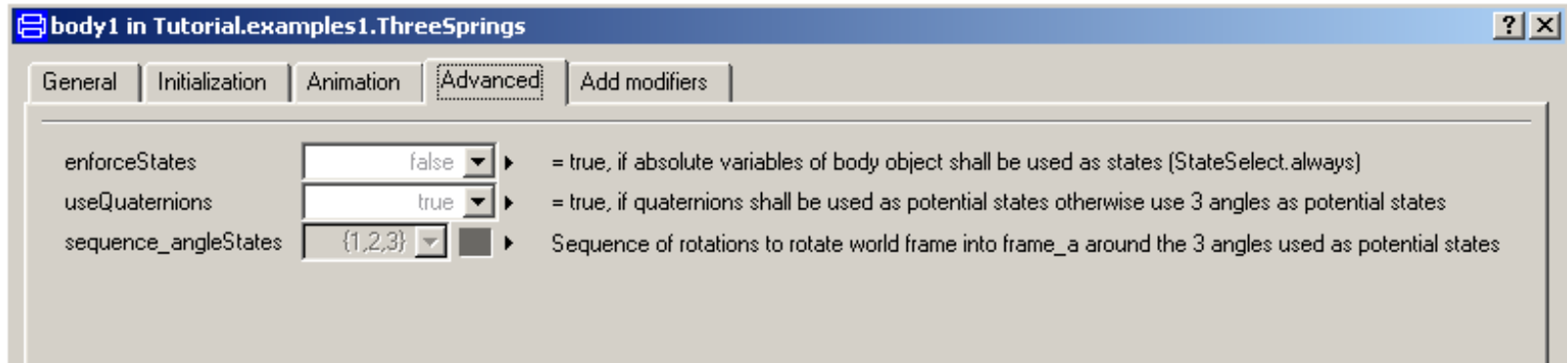
- here: body coordinates: position, quaternions and their derivatives are used as states

Modelica Multibody Advanced: State selection II

- relative joint coordinates are used as states if possible
 - default: stateSelect = StateSelect.prefer
 - e.g. Multibody.Joints.Prismatic



```
final parameter Real e[3]=Modelica.Mechanics.MultiBody.Frames.normalize(n)
  "Unit vector in direction of prismatic axis n";
SI.Position s(stateSelect=if enforceStates then
  StateSelect.always else StateSelect.prefer)
  "Relative distance between frame_a and frame_b";
SI.Velocity v(stateSelect=if enforceStates then StateSelect.always else
  StateSelect.prefer) "First derivative of s (relative velocity)";
```

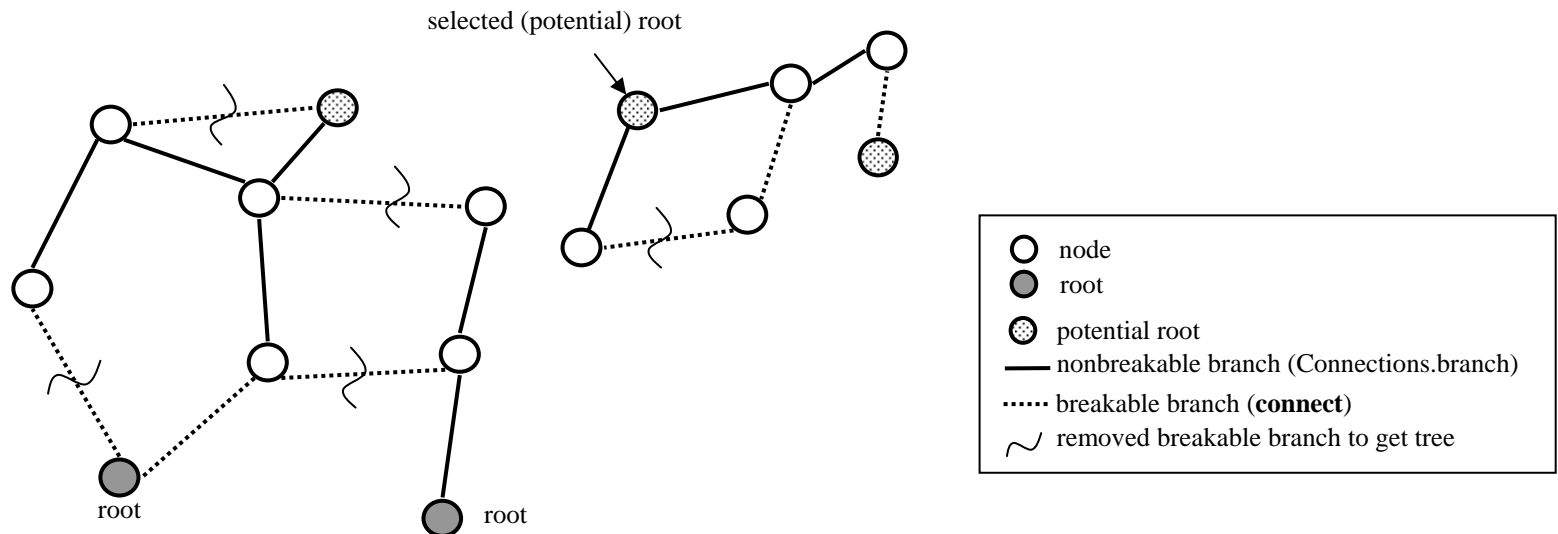


- Advanced user may influence state selection directly

Modelica Multibody Advanced: Loops I

➤ Standard case

- no specific action by the user is required
- every connector is one node in the virtual connection graph
- roots of the virtual connection graph are found, e.g. `world.frame_b`
- loops are virtually broken



Modelica Multibody Advanced: Loops I

➤ Standard case

- no specific action by the user is required
- every connector is one node in the virtual connection graph
- roots of the virtual connection graph are found, e.g. world.frame_b
- loops are virtually broken
- the related constraint equations are provided

⇒ DAE

$$0 = f(\dot{x}, x, y, t, \dots) \quad \dim(f) = \dim(x) + \dim(y)$$

- Equations are rearranged to get a sequence for model evaluation
(**B**lock **L**ower **T**riangle-partitioning)

$$\begin{array}{l} f_1 \\ f_2 \\ f_3 \\ f_4 \\ f_5 \end{array} \begin{pmatrix} z_1 & z_2 & z_3 & z_4 & z_5 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 1 \end{pmatrix} \Rightarrow \begin{array}{l} f_2 \\ f_4 \\ f_3 \\ f_5 \\ f_1 \end{array} \begin{pmatrix} z_1 & z_2 & z_3 & z_4 & z_5 \\ 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 \end{pmatrix}$$

Modelica Multibody Advanced: Loops I

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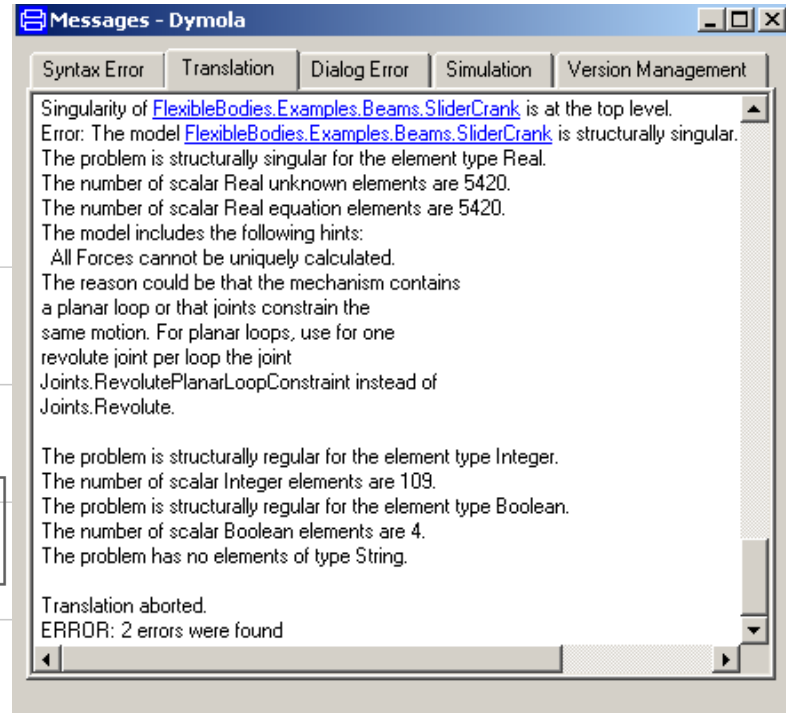
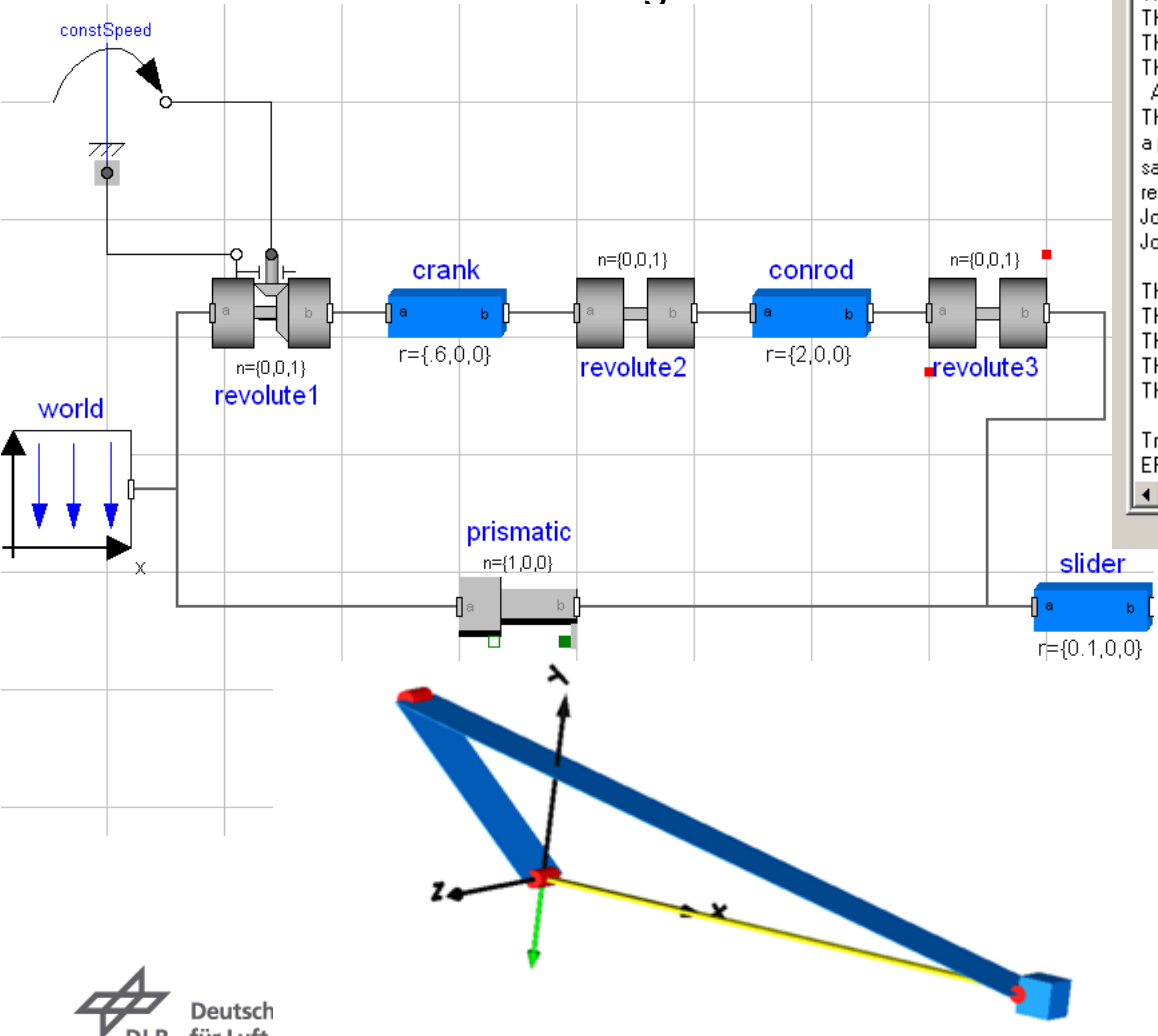
- Equations are rearranged to get a sequence for model evaluation (**B**lock **L**ower **T**riangle-partitioning)
- Equations to be differentiated are determined (Pantelides algorithm)
- superfluous potential states are deselected dynamically (dummy derivative method) ⇒ ODE:

$$\dot{x} = f(x, t, \dots)$$

Modelica Multibody Advanced: Loops III

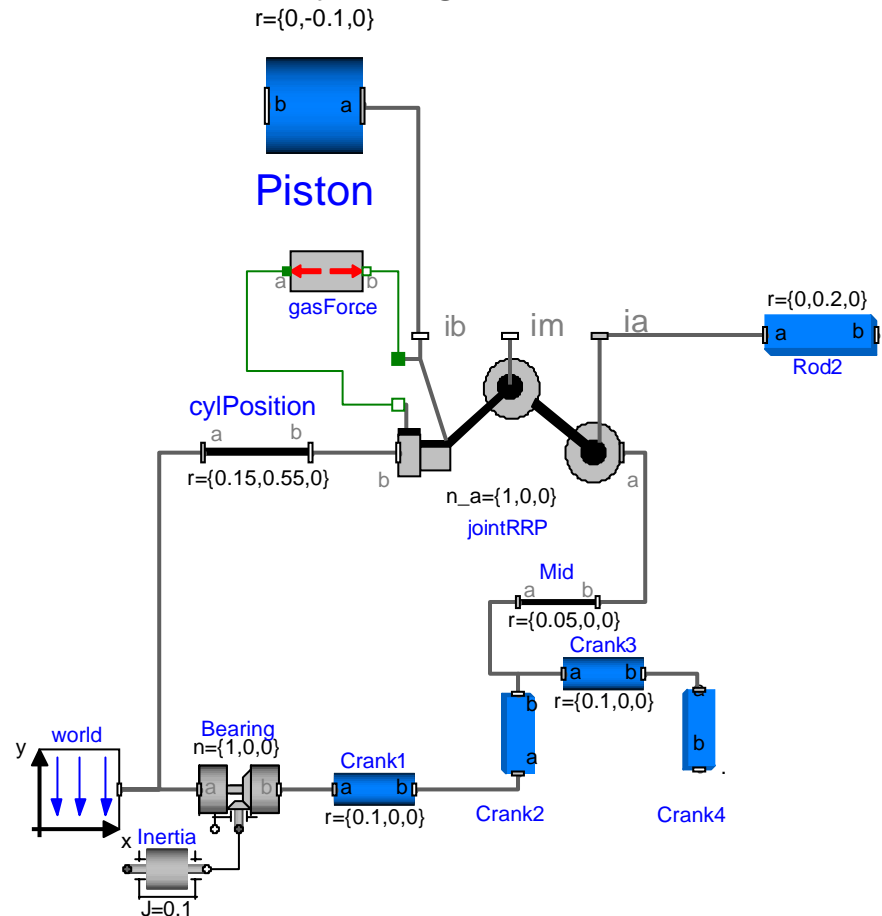
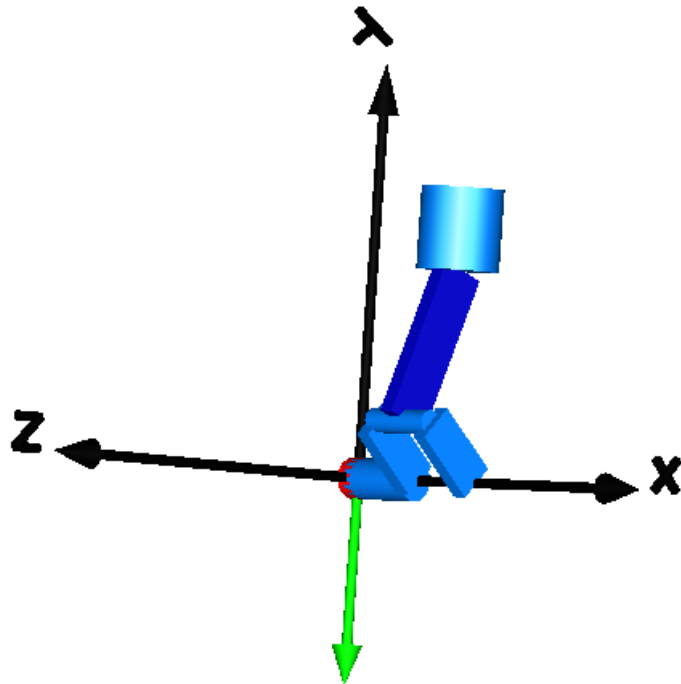
➤ Planar loops

➤ error message



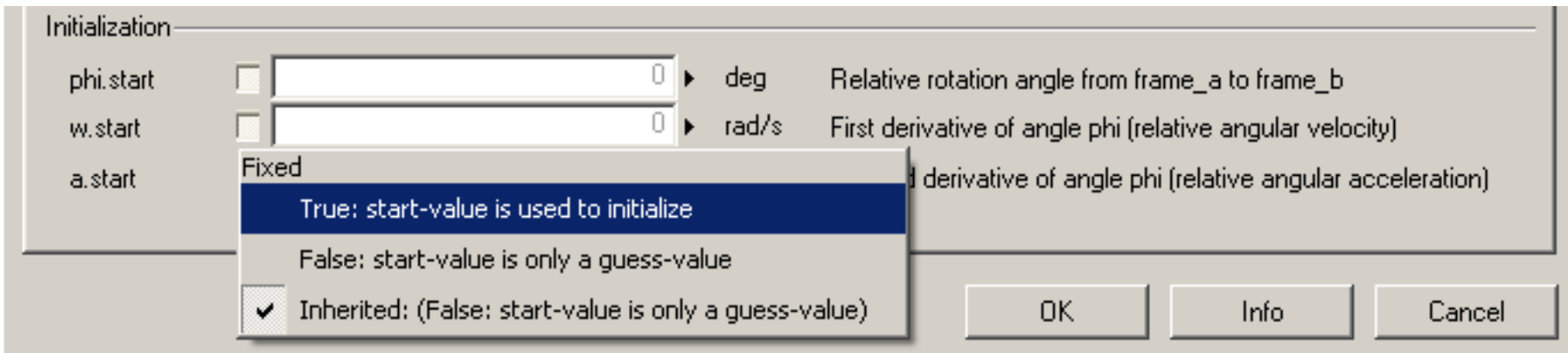
Modelica Multibody Advanced: Loops IV

- Use of aggregated joint objects
 - to profit from analytical loop handling according to the „characteristic pair of joints“ method by the group of Prof. Hiller



Modelica Multibody Advanced: Initialisation

- Initialisation default:
 - every state is assumed to be arbitrary unless otherwise provided
 - Newton solver starts with guess value zero in order to find consistent initial states unless otherwise provided
- If initialisation fails
 - determine, i.e. fix, characteristic variables/states in order to influence the system of equations to solve
 - provide „good“ guesses for initial states
 - be aware of singular positions, e.g. piston at bottom dead center
 - keep initialisation system consistent



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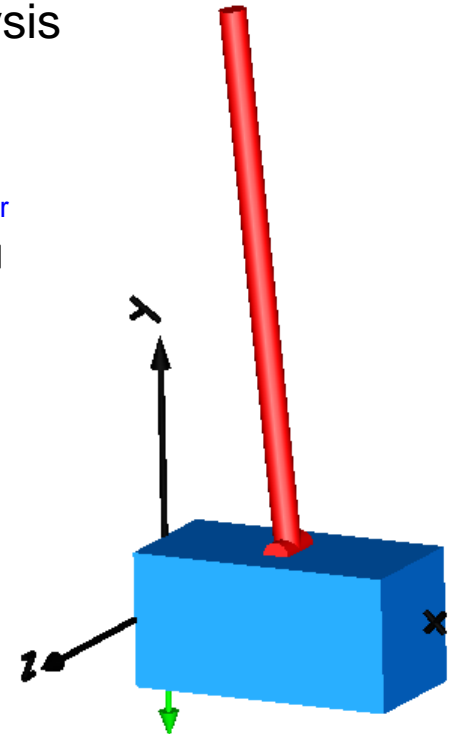
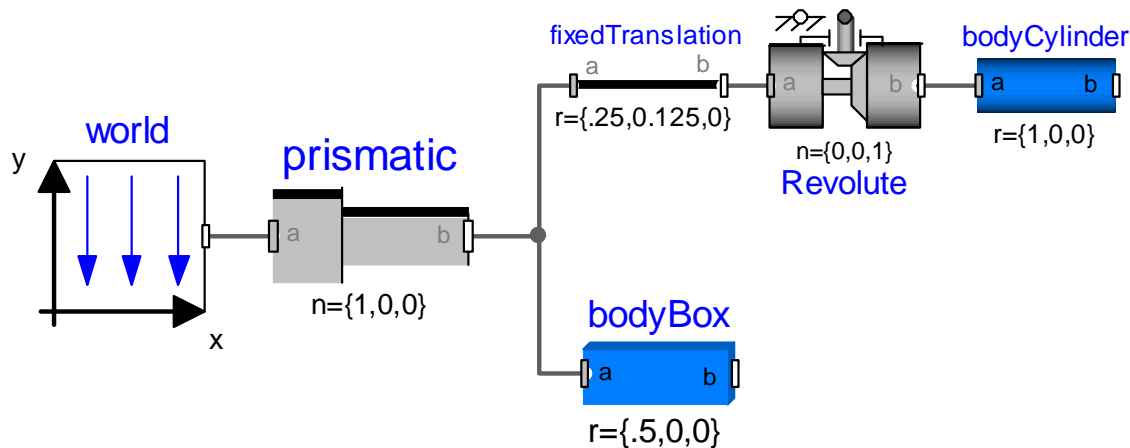
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Example 1: Control of an inverse pendulum I

➤ Initial model

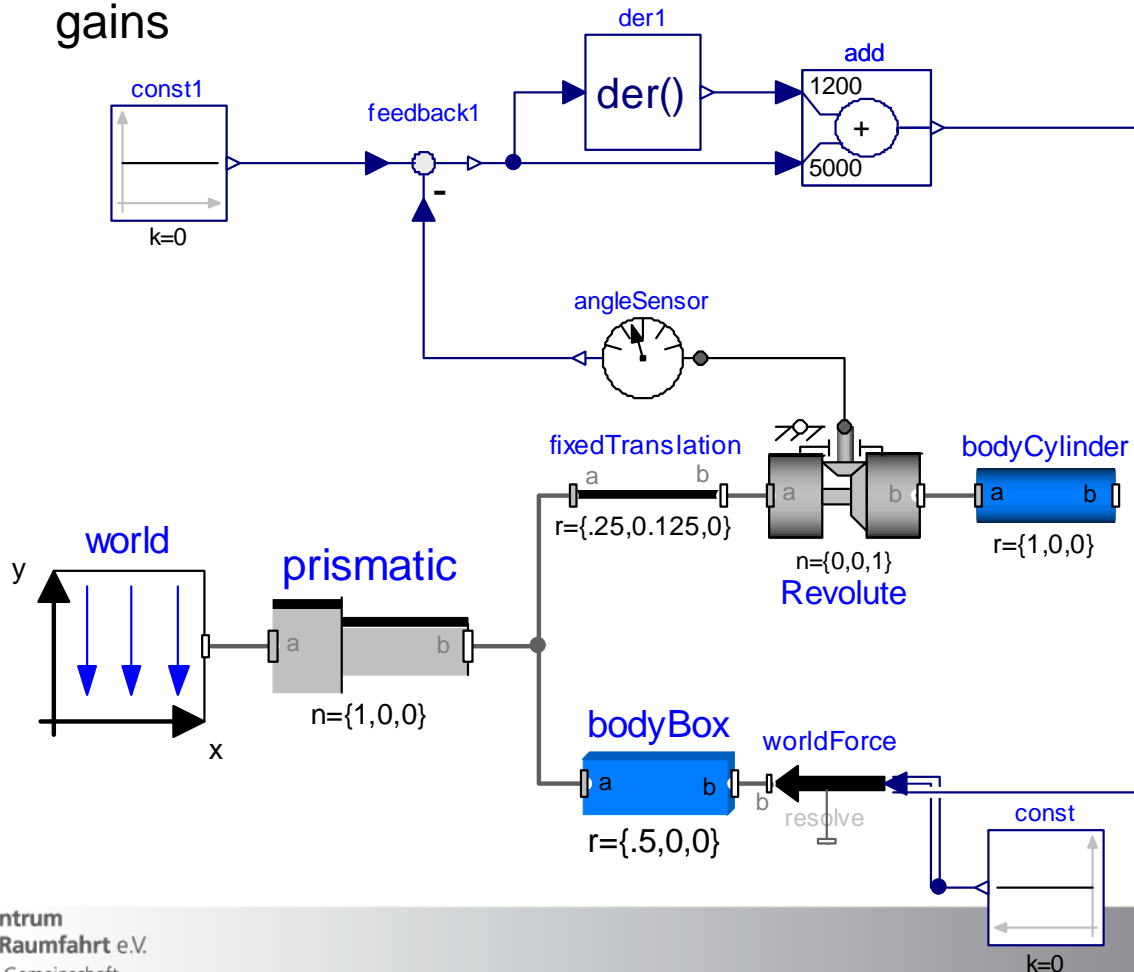
- Box: 0.5 x 0.25 x 0.25 m
- actuatedRevolute: 90° phi_offset, 5° phi_start
- perform time simulation and eigenvalue analysis



Example 1: Control of an inverse pendulum II

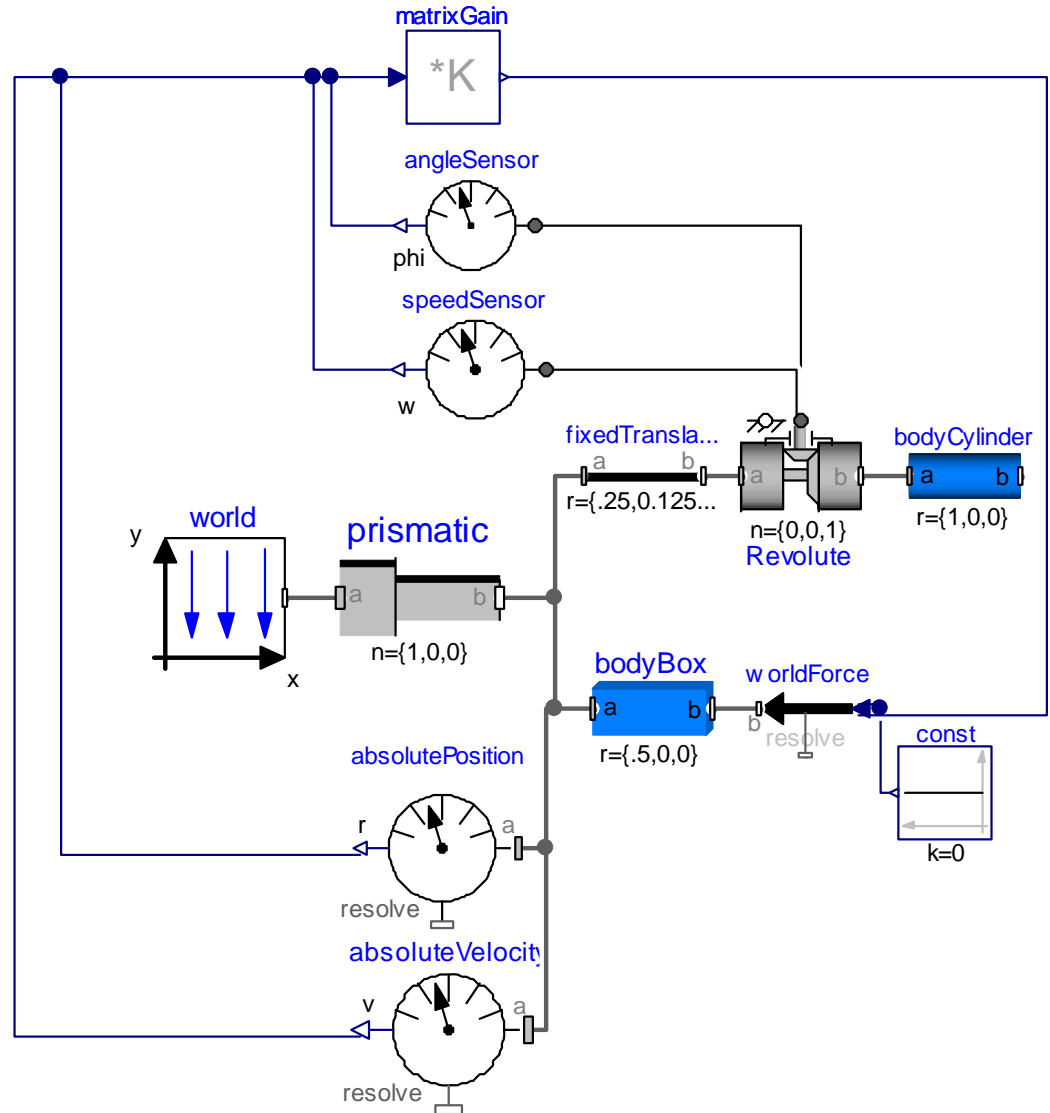
➤ PD-Control of angle only

- use extend to inherit initial model
- use transient response and pole placement to set-up controller gains



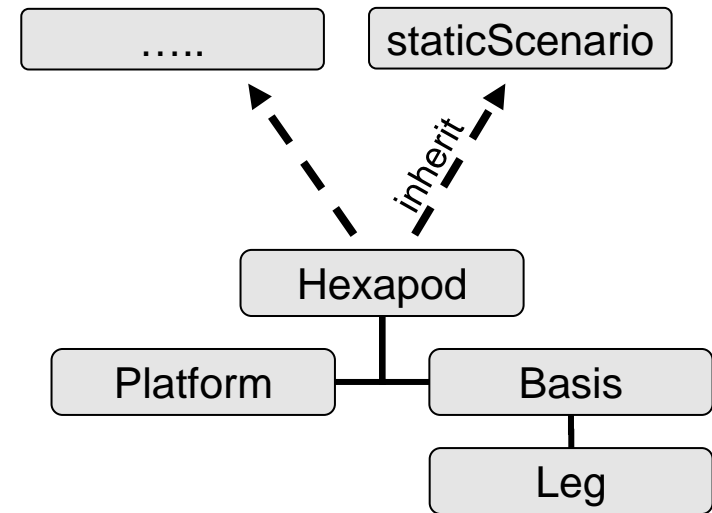
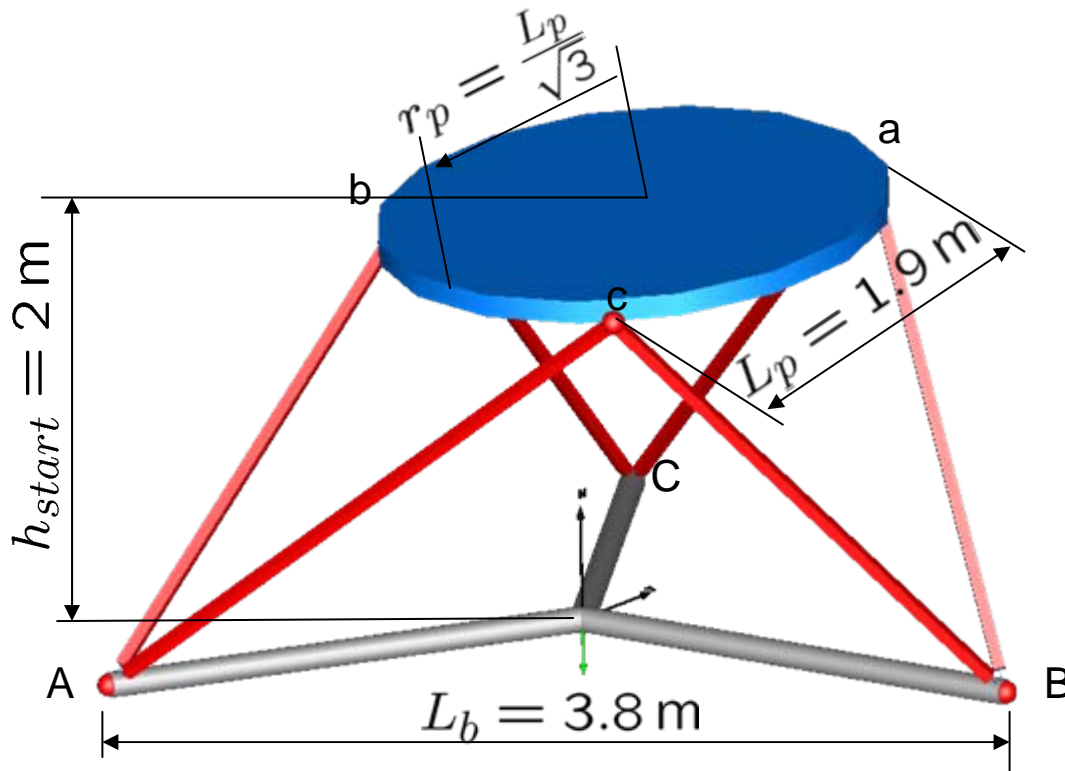
Example 1: Control of an inverse pendulum III

- Improve control
 - e.g. state control



Exercise 2: Hexapod I

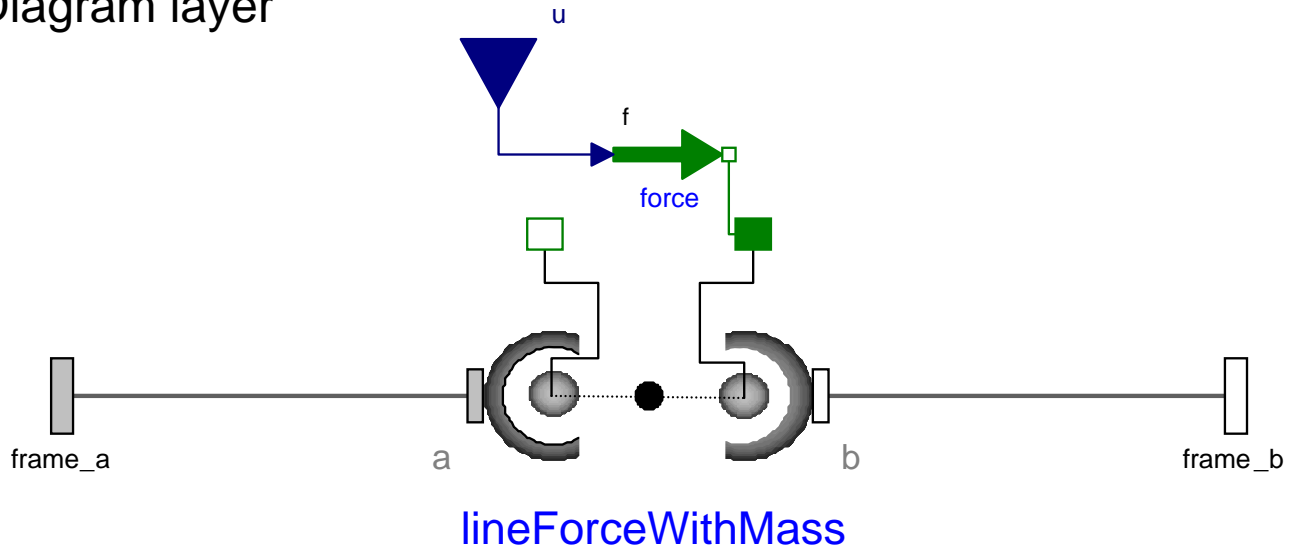
➤ The modelling concept



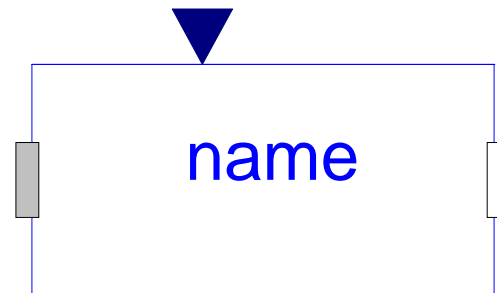
Exercise 2: Hexapod II

➤ Model Leg

➤ Diagram layer



➤ Icon layer



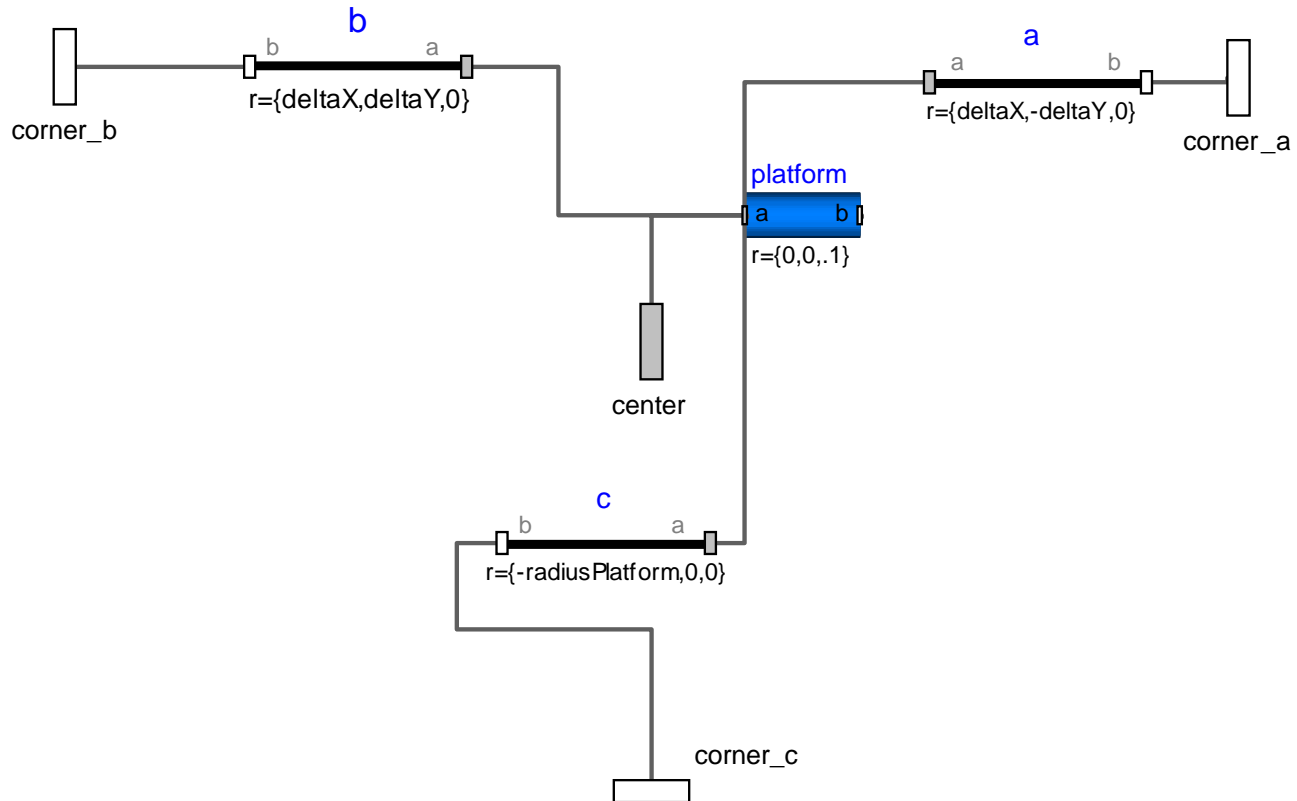
Exercise 2: Hexapod III

➤ Model Platform

```

model Platform
  import SI = Modelica.SIunits;
  parameter SI.Length Lp=1.9 " length of a side of the platform";
  final parameter SI.Length radiusPlatform=Lp/sqrt(3);
  final parameter SI.Length deltaX=radiusPlatform/2;
  final parameter SI.Length deltaY=Lp/2;

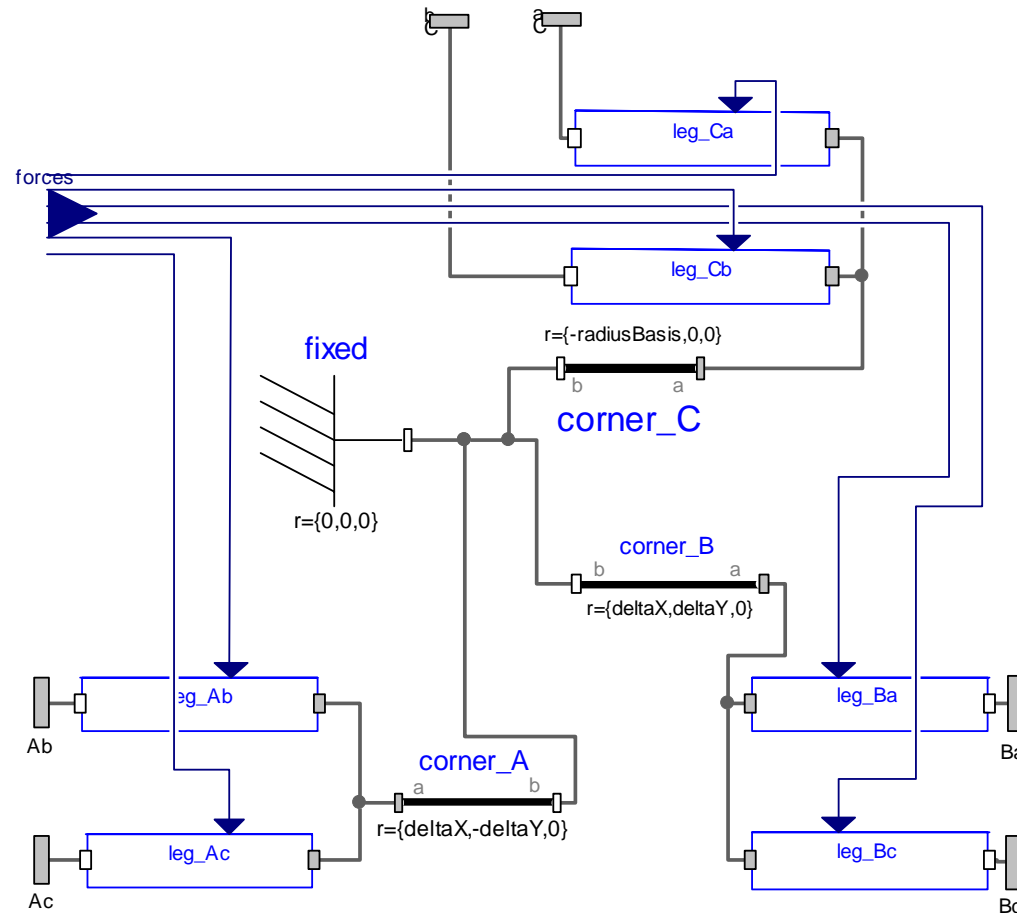
```



Exercise 2: Hexapod IV

➤ Model Basis

```
model Basis
  import SI = Modelica.SIunits;
  parameter SI.Length Lb=3.8 " length of a side of the basis";
  final parameter SI.Length radiusBasis=Lb/sqrt(3);
  final parameter SI.Length deltaX=radiusBasis/2;
  final parameter SI.Length deltaY=Lb/2;
```

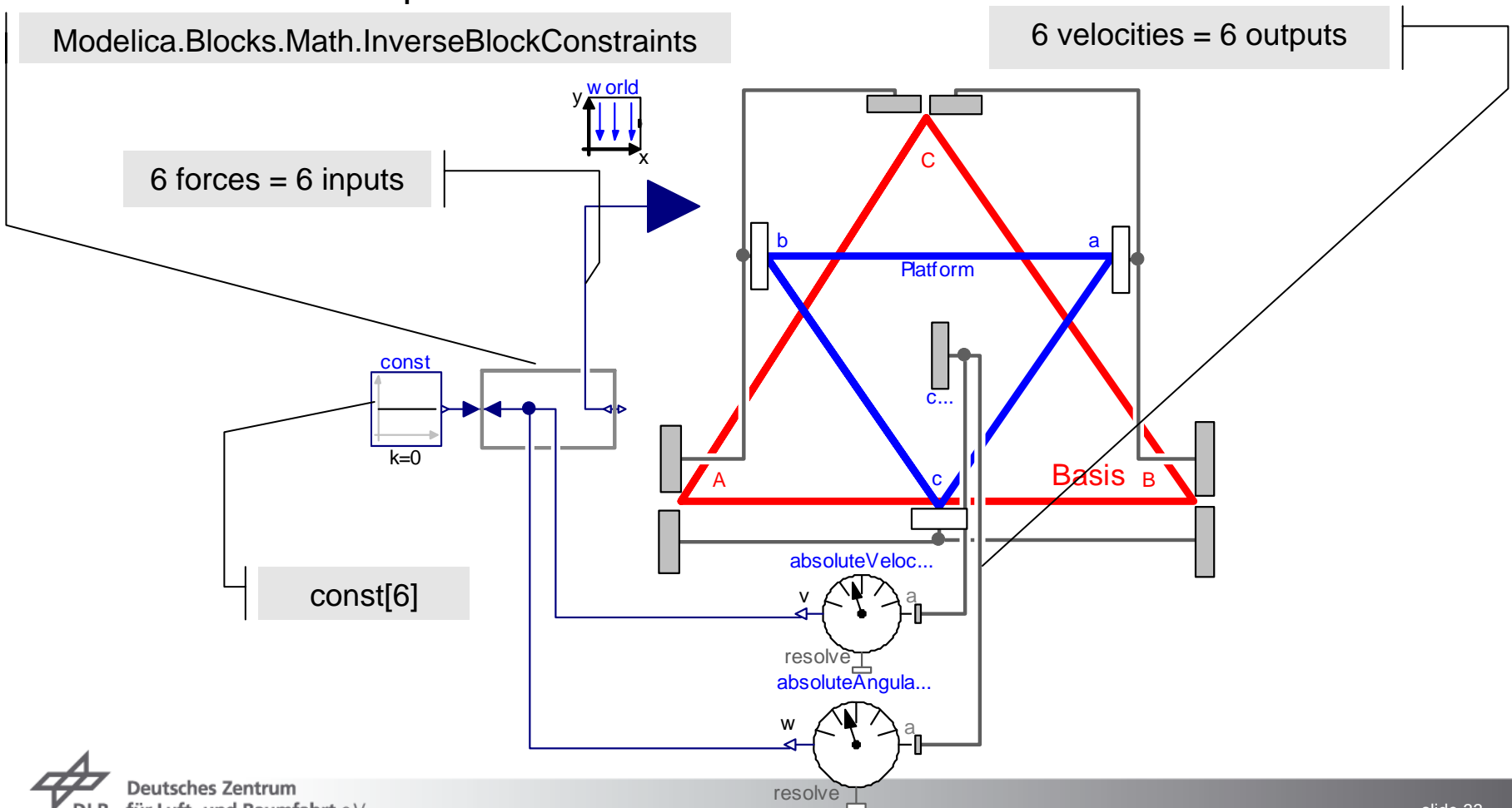


Exercise 2: Hexapod V

- Hexapod_StaticScenario
 - actuator force in initial position ?

```

partial model Hexapod
import SI = Modelica.SIunits;
parameter SI.Length h_start=2;
    
```

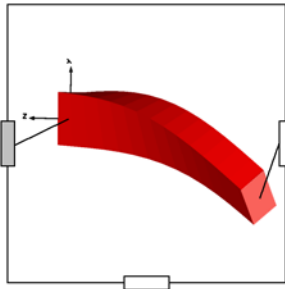


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FlexibleBodies Library: Beams versus ModalBody

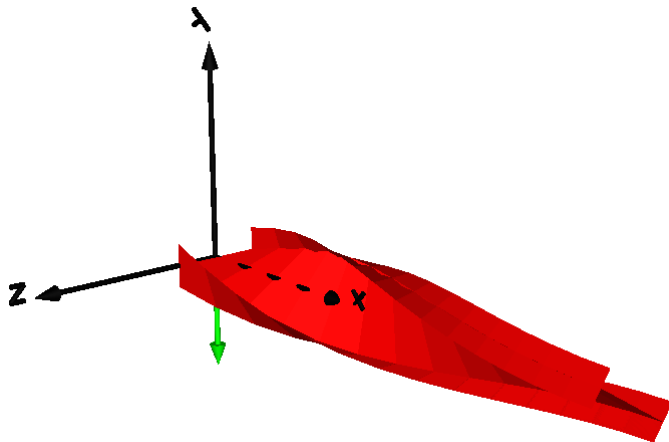
beam



Analytical beam description

Modelica generated SID

Animation uses beam description



Common Issues

Floating frame of reference

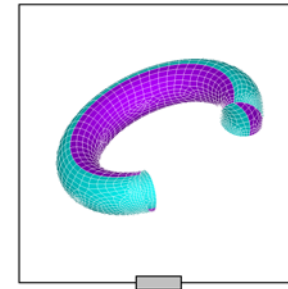
Equations of motion

SID-data-structure

Standard-Input-Data: Wallrapp '94

Disjunctive Issues

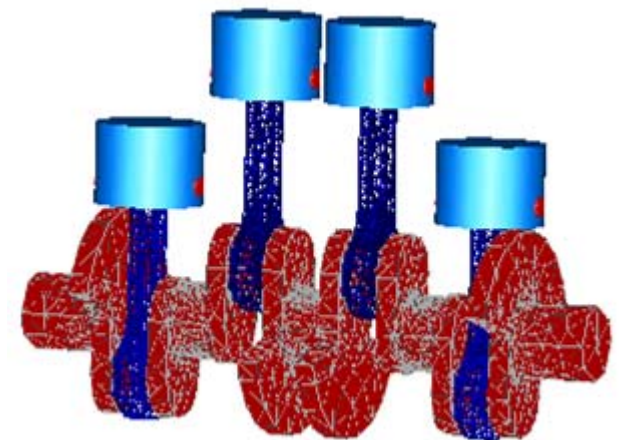
modalBody



FEM-based body description

External generated SID

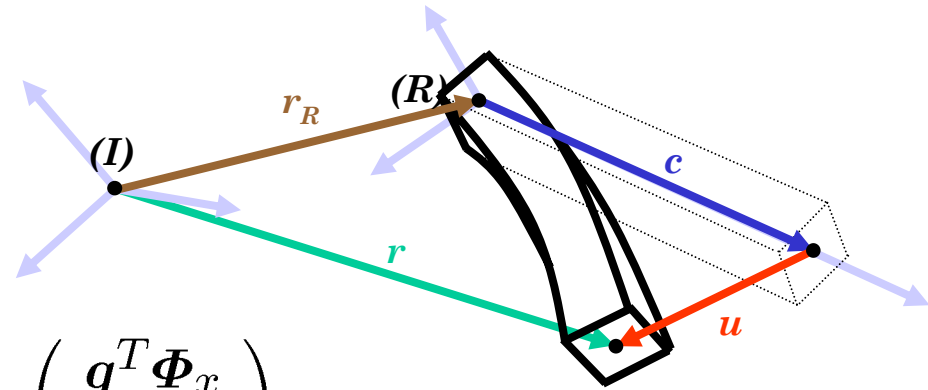
Animation based on external data



FlexibleBodies Library: Equations of motion

- Floating frame of reference

$$\mathbf{r} = \mathbf{r}_R + \mathbf{c} + \mathbf{u}$$



- Modal approach

$$\mathbf{u}(\mathbf{c}, t) = \Phi(\mathbf{c}) \mathbf{q}(t) + \frac{1}{2} \begin{pmatrix} \mathbf{q}^T \Phi_x \\ \mathbf{q}^T \Phi_y \\ \mathbf{q}^T \Phi_z \end{pmatrix} \mathbf{q}$$

- Equations of motion

$$\begin{pmatrix} m\mathbf{I}_3 & & \text{sym.} \\ m\tilde{\mathbf{d}}_{CM} & \mathbf{J} & \\ \mathbf{C}_t & \mathbf{C}_r & \mathbf{M}_e \end{pmatrix} \begin{pmatrix} \mathbf{a}_R \\ \boldsymbol{\alpha}_R \\ \ddot{\mathbf{q}} \end{pmatrix} = \mathbf{h}_\omega - \begin{pmatrix} 0 \\ 0 \\ \mathbf{K}_e \mathbf{q} + \mathbf{D}_e \dot{\mathbf{q}} \end{pmatrix} + \begin{pmatrix} \mathbf{f}_a \\ \mathbf{f}_\alpha \\ \mathbf{f}_q \end{pmatrix}$$

Bremer/Pfeiffer '92, Schwertassek/Wallrapp '99

FlexibleBodies Library: Beam theory

➤ 2nd order displacement field

➤ bending in xy- und xz- plane, torsion and lengthening

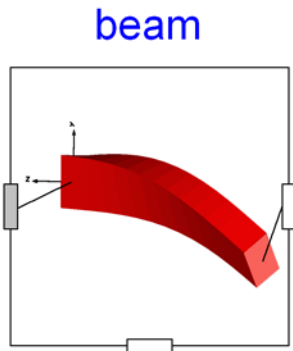
$$\mathbf{u}(x, t) = \begin{pmatrix} u \\ v \\ w \end{pmatrix} + \begin{pmatrix} -\frac{1}{2} \int_0^x v'^2 + w'^2 dx \\ -\int_0^x \int_0^{\bar{x}} \theta w'' d\bar{x} d\bar{x} + \int_0^x u'v' d\bar{x} \\ \int_0^x \int_0^{\bar{x}} \theta v'' d\bar{x} d\bar{x} + \int_0^x u'w' d\bar{x} \end{pmatrix}$$

➤ Raleigh-Ritz-approach for a straight, homogenous, isotropic beam with constant cross section

➤ expansion with analytic eigenvalue-solutions of the Euler-Bernoulli beam

$$v(x, t) = \Phi_v(x) \mathbf{q}_v(t) \quad \Phi_i = \begin{pmatrix} \cosh(\tau_i x) \\ \sinh(\tau_i x) \\ \cos(\tau_i x) \\ \sin(\tau_i x) \end{pmatrix}^T \begin{pmatrix} c_1 \\ c_2 \\ c_3 \\ c_4 \end{pmatrix}_i$$

FlexibleBodies Library: Beam menu set-up I



data in FlexibleBodies.Examples.Demo

General Add modifiers

Component

Name data

Comment

Model

Path FlexibleBodies.Interfaces.BeamData

Comment

Parameters

crossSection I_beam

l 1.58 m length of beam

rho 7850 kg/m³ mass density

E 2.1e11 N/m² Young's modulus

G E/(2*(1 + 0.3)) N/m² Shear modulus

xsi {5} specification of int

Eigenmodes

bending_xy ryConditionB=FlexibleBodies.Types.BoundaryCondition.F

bending_xz ryConditionB=FlexibleBodies.Types.BoundaryCondition.F

torsion ryConditionB=FlexibleBodies.Types.BoundaryCondition.F

lengthening ryConditionB=FlexibleBodies.Types.BoundaryCondition.F

Parameters

crossSection I_beam

l 1.58 m

rho 7850 kg/m³

E 2.1e11 N/m²

G E/(2*(1 + 0.3)) N/m²

xsi {5}

Eigenmodes

bending_xy T_beam

bending_xz T_beam

general

Icon

BeamData

I_beam crossSection

I_beam

Description

I-profile cross section

Inputs

width .02 m outer contour dimension in y-direction (along flange)

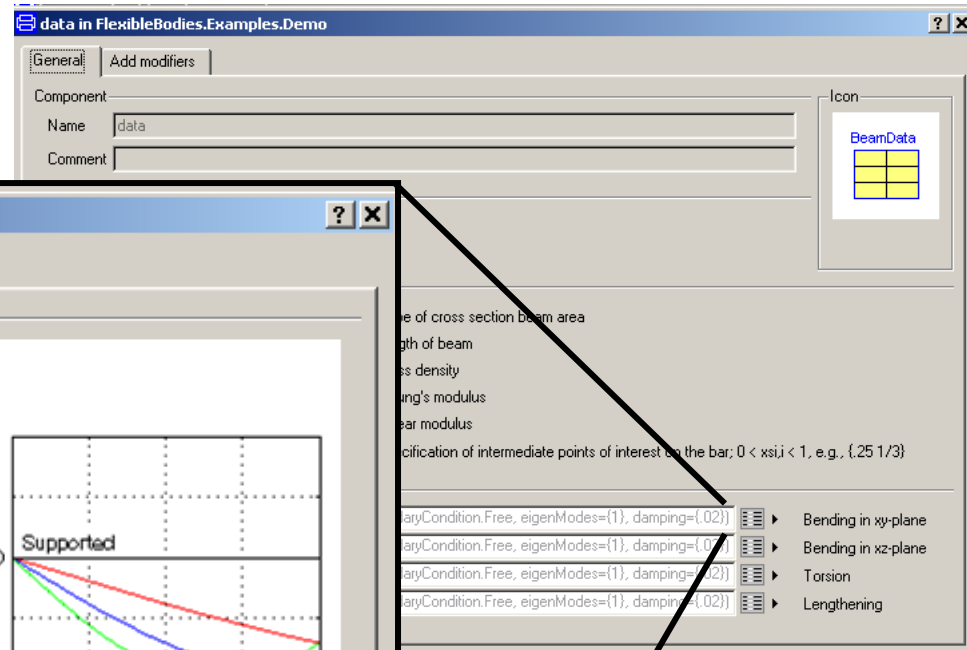
t_bar 0.001 m thickness of central bar

height .03 m outer contour dimension in z-direction

t_flange 0.001 m thickness of flanges

OK Info Close

FlexibleBodies Library: Beam menu set-up II



BeamModeData bending_xz

BeamModeData

Mode Shapes due to Boundary Conditions

Boundary Conditions

at frame_a Free Clamped Supported ▶

at frame_b Free Clamped Supported ▶

Mode Numbers

eigenModes {1,2,4} Ordinal numbers of eigen modes to be used (e.g.

damping {0.01,0.03,0.02} Damping of eigen modes

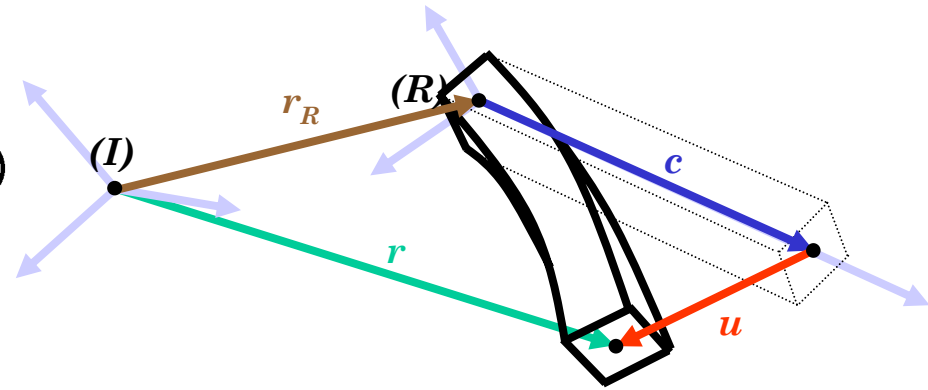
$$\Phi_i = \begin{pmatrix} \cosh(\tau_i x) \\ \sinh(\tau_i x) \\ \cos(\tau_i x) \\ \sin(\tau_i x) \end{pmatrix}^T \begin{pmatrix} c_1 \\ c_2 \\ c_3 \\ c_4 \end{pmatrix}_i$$

mandatory to define as much damping coefficients as modes

FlexibleBodies Library: Boundary Conditions I

- Mechanical interpretation

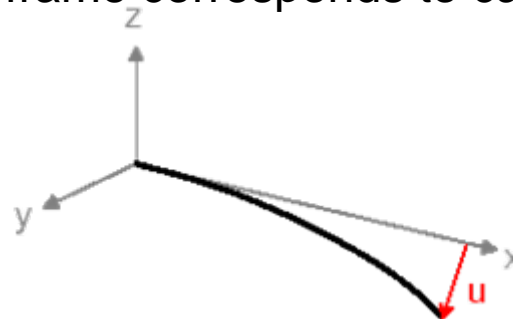
$$\mathbf{r}(\mathbf{c}, t) = \mathbf{r}_R(t) + \mathbf{c} + \mathbf{u}(\mathbf{c}, t)$$



- let's say: frame of reference is pinned at frame_a with $\mathbf{c} = \mathbf{0}$
 - ⇒ motion of frame_a is completely described by $\mathbf{r}_R(t)$ (and related orientation)

$$\Rightarrow \mathbf{u}(\mathbf{c} = \mathbf{0}, t) = \mathbf{0} \quad \frac{\partial \mathbf{u}}{\partial \mathbf{c}}(\mathbf{c} = \mathbf{0}, t) = \mathbf{0}$$

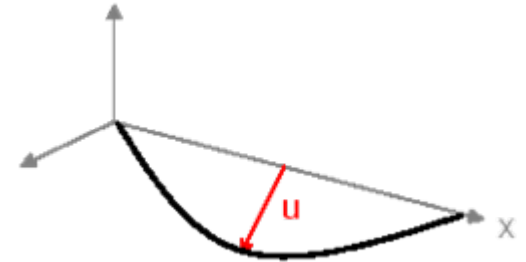
- clamped-free: tangent frame corresponds to cantilever beam boundary conditions



FlexibleBodies Library: Boundary Conditions II

- supported-supported: chord frame

$$u(c = 0, t) = 0 \quad u(c = (l, 0, 0), t) = 0$$



- free-free: Buckens frame

- linear and angular momentum due to body deformation are zero

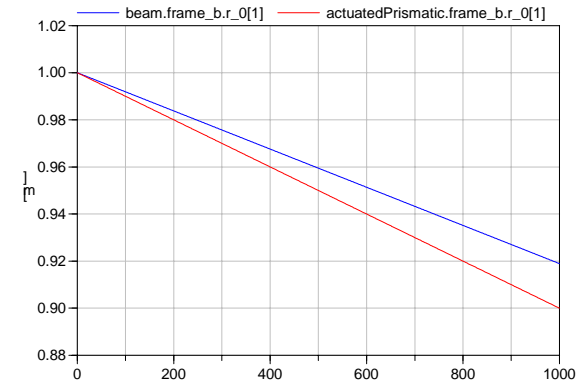
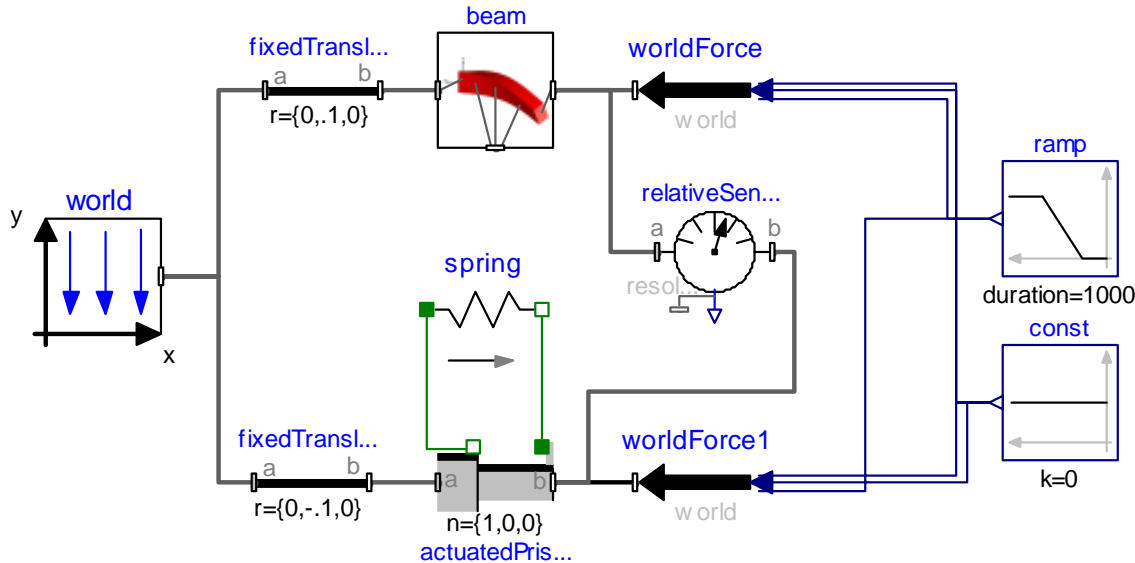
- every combination of tangent, chord and Buckens frames in different spatial directions is possible

- General rule

- align the boundary conditions with the degree of freedom of the joints to which the beam is attached
 - boundary conditions are related to constraint forces
 - a joint cannot transmit a constraint force in the direction of its motion
- BUT: Boundary conditions are validation issues

FlexibleBodies Library: A classic pitfall I

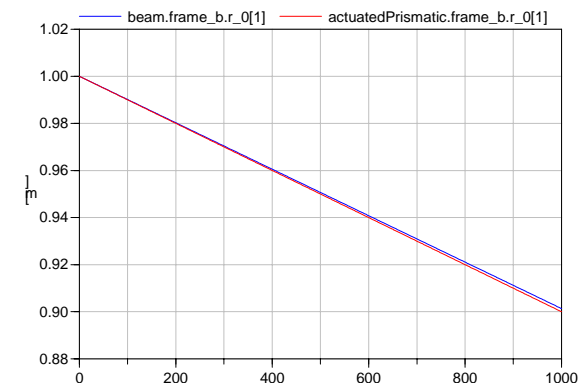
➤ static deflection: thrust force shortens beam and equivalent spring



1 eigenmode

	spring	beam	error
1 eigenmode	-10 cm	-8.1 cm	19 %
5 eigenmodes	-10 cm	-9.6 cm	4 %
10 eigenmodes	-10 cm	-9.8 cm	2 %
15 eigenmodes	-10 cm	-9.9 cm	1 %

comparison: deflections at the end



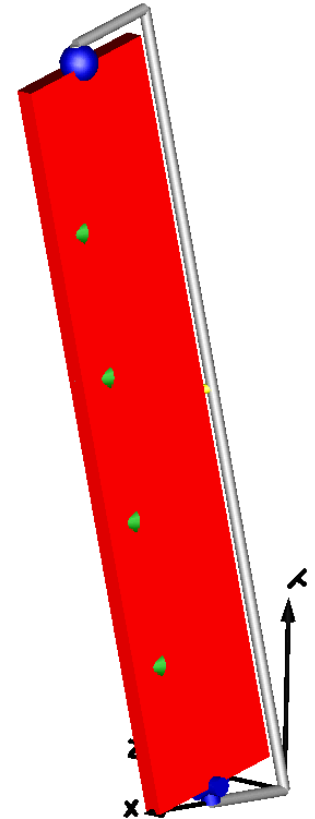
15 eigenmodes

FlexibleBodies Library: A classic pitfall II

- Mechanical background
 - static deflections rely on elastic properties only
 - eigenmodes consider elastic and inertia properties
 - that's why they are well suited for dynamic problems
- Geometrical background
 - analytically: $u = c \cdot x$
 - expansion with eigenmodes: $u = \sin\left(\frac{2x}{\pi l}\right) + \sin\left(\frac{2x}{3\pi l}\right) + \dots$
- It is proven that Raleigh-Ritz approach converges against true value
 - but how fast ?
 - this is an extreme example, e.g. bending is less sensitive
- Check whether a higher number of modes changes results !

Example 3: AircraftFin

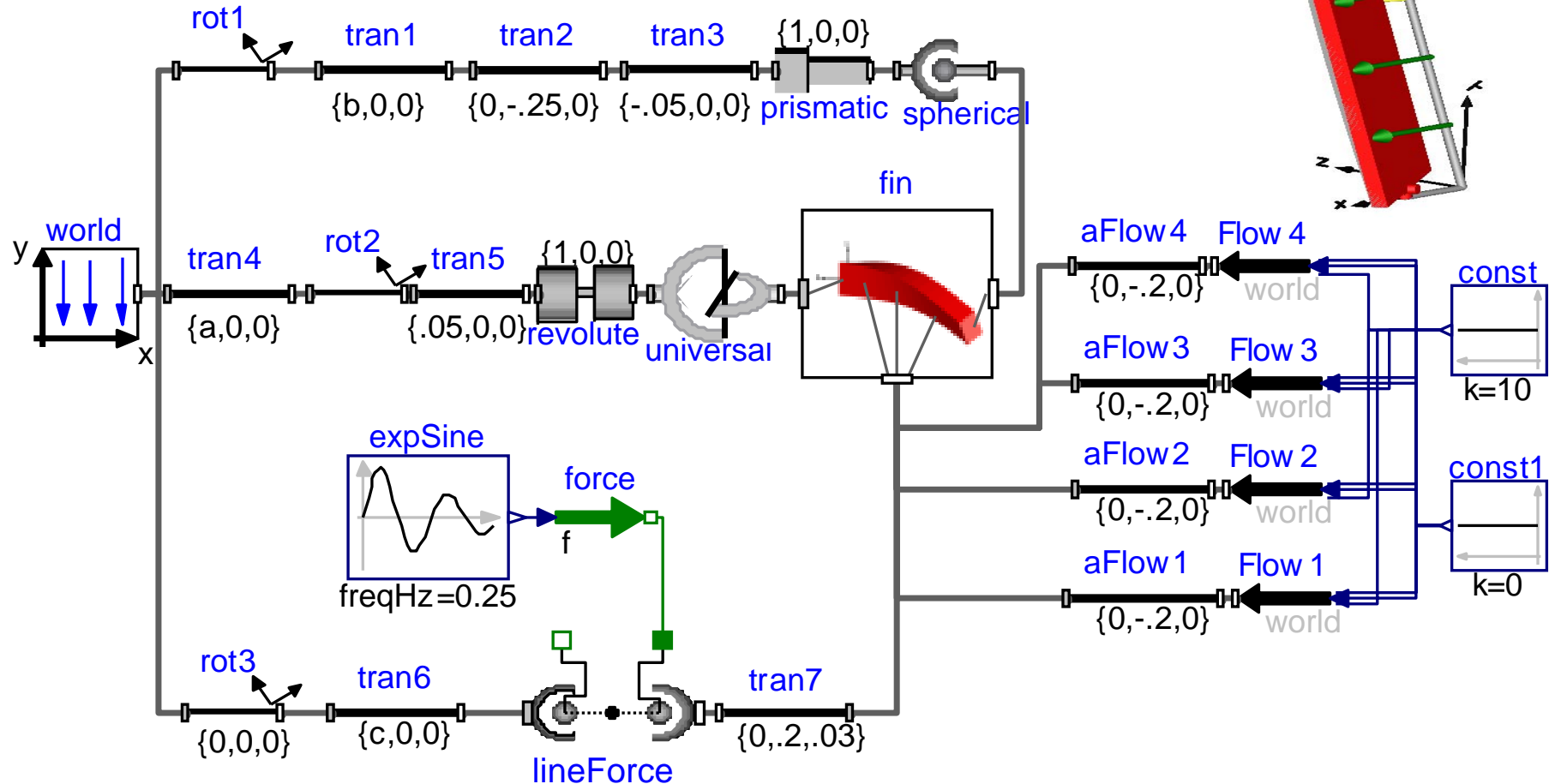
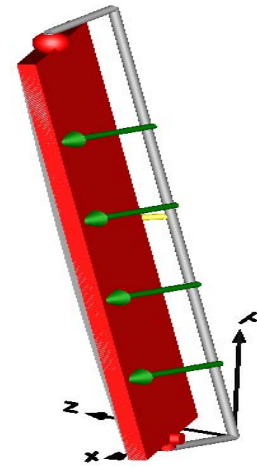
- fin
 - mounted in a frame with 15° inclination
 - profil: squarepipe $0.4 \times 0.05 \times 0.01$ m
 - 2 m long
 - 2730 kg/m^3 , $7 \cdot 10^{10} \text{ N/m}^2$ (aluminium)
 - 1 xz-bending and 1 torsion mode
 - 5 mid-nodes $\xi = \{0.2, 0.4, 0.5, 0.6, 0.8\}$
- actuator to turn the fin
(force as cos-function of t, 1 Hz, 10 N amplitude)
- 4 constant forces, 10 N in world-x-direction,
to represent flow forces



```
model AircraftFin
```

```
import Modelica.Constants.pi;  
parameter Real a= 0.25/cos(pi/12);  
final parameter Real b=a*sin(pi/12)+2.1;  
final parameter Real c=a*sin(pi/12)+1.05;
```

Example 3: AircraftFin



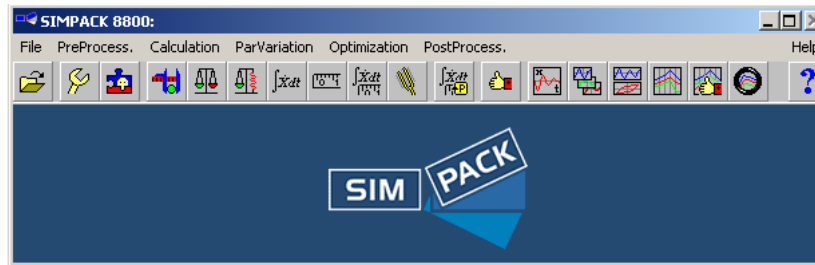
Contents

- Modelica Multibody Basics
- Modelica Multibody Advanced
- Exercise 1: Control of an inverse pendulum
- Exercise 2: Hexapod
- FlexibleBodies Library: Beams
- Exercise 3: Aircraft Fin
- FlexibleBodies Library: General bodies based on finite element data
- Exercise 4: Rod



FlexibleBodies Library: FEM-preprocessing

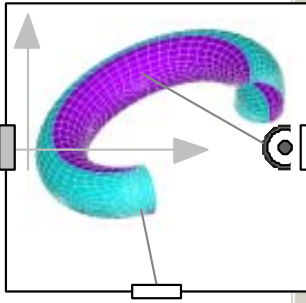
- Simpack-FEMBS: FEM to multibody system preprocessor
- Maintained and distributed by INTEC GmbH, Oberpfaffenhofen



- Supports ABAQUS, ANSYS, MSC.Nastran, NX Nastran, I-DEAS, PERMAS
- Reduction of the FE-model in 2 steps
 - in FE-tool, e.g. Guyan- or Craig-Bampton-method
 - ⇒ system matrices, nodes to retain, eigenmodes, mesh information
 - in Simpack-FEMBS
 - ⇒ modes selection (and generation), multibody description, animation data
- SID- and wavefront-file as results

FlexibleBodies Library: ModalBody menu set-up I

modalBody



modalBody in FlexibleBodies.Examples.ModalBodies.Internal.CylinderElasticRodPiston

General Initialization Advanced Add modifiers

Component

Name modalBody

Comment

Model

Path FlexibleBodies.ModalBody

Comment General flexible body model based on a modal description

Icon

ModalBody

Parameters

SID_fileName FlexibleBodies.Utilities.DataDirectory + "rodV2.SID_FEM" File name of SID file describing the flexible body dynamics

WavefrontFile FlexibleBodies.Utilities.DataDirectory + "rodV2small.obj" File name of wavefront file describing the flexible body animation

Simulation nodes (= subset of finite element nodes) associated with connectors nodes_sphericalJoint and nodes_clamped

sphericalJointNodes {20001,20002} Simulation nodes of nodes_sphericalJoint (= do not constrain rotation)

clampedNodes fill(0, 0) Simulation nodes of nodes_clamped (= constrain translation and rotation)

Animation

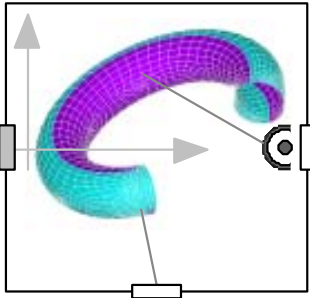
Solid animation Exaggeration factor to visualize deformation 1 Color {0,0,255} Specular coefficient 0.7

Wire frame animation Exaggeration factor to visualize deformation 200 Color {155,155} Specular coefficient 0

OK Info Cancel

FlexibleBodies Library: ModalBody menu set-up II

modalBody

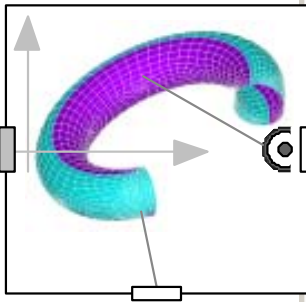


Variables	Values	Unit
ShowSimulationNodes 1		
ShowSimulationNodes 2		
world		
modalBody		

```
Selected object: world.frame_b_r_0[1]
Selected object: modalBody.Animation.Form
Simulation Node: 20001
Hidden.ShowSimulationPoints = true
```

FlexibleBodies Library: ModalBody menu set-up II

modalBody



rod in FlexibleBodies.Tutorial.Exercises.Rod

General Initialization **Advanced** Add modifiers

enforceStates ▶ = true, if elastic joint coordinates shall be used as states

useQuaternions ▶ = true, if quaternions shall be used as potential states otherwise use 3 angles as potential states

sequence_angleStates ▶ Sequence of rotations to rotate world frame into frame_a around the 3 angles used as potential states

Nominal

q_nominal ▶ Nominal values of generalized coordinates (for numerical scaling)

qd_nominal ▶ Nominal values of generalized velocities (for numerical scaling)

Structural damping

dampingCoefficients ▶ Natural damping coefficients

userDamping ▶ = true, if structural damping parameters shall be redefined (and taken instead of values in the SID-file)

Nodes Presentation

Node axes animation ▶ Length to present of axes at nodes m ▶

Axes Colors: of frame_ref ▶ of nodes_clamped ▶ of nodes_sphericalJoint ▶

OK Info Cancel

FlexibleBodies Library: 4 Cylinder Engine

➤ FEM

➤ Crankshaft 85 342 nodes

➤ Piston rod 12531 nodes

➤ Multibody representation

➤ < 1900 Hz

➤ Crankshaft

➤ 2 torsion eigenmodes

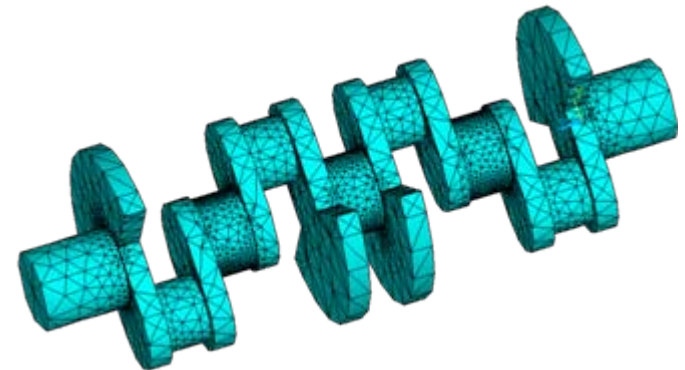
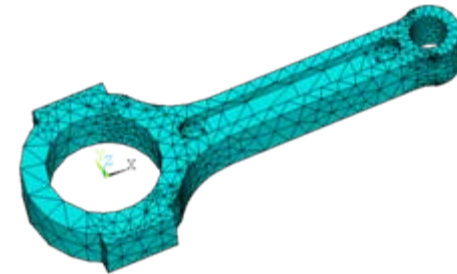
➤ 273 simulation nodes

➤ Piston rod

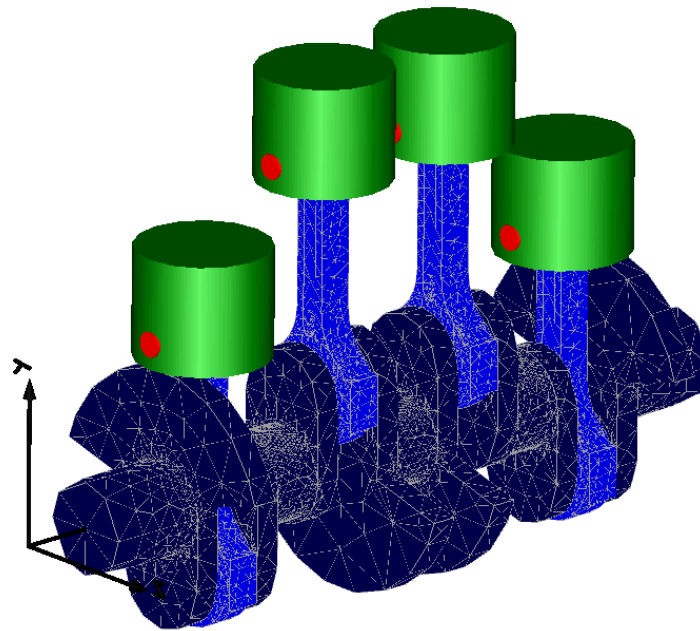
➤ 4 eigenmodes each

➤ 120 simulation nodes

➤ Time integration with gas force, 38 states, ≈ 6 cpu-s per s



FlexibleBodies Library: 4 Cylinder Engine II



Contents

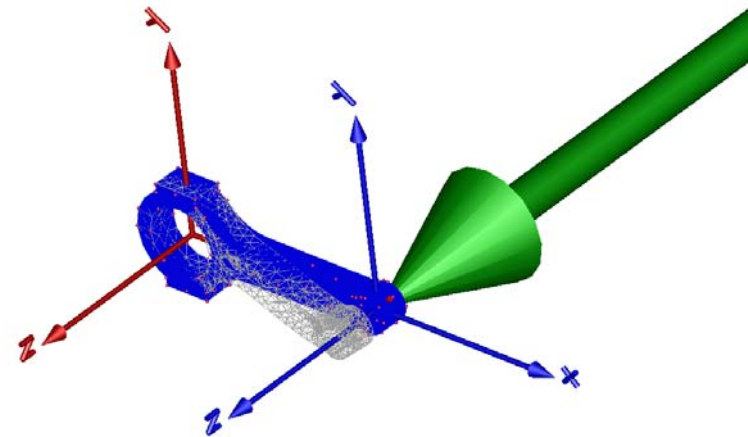
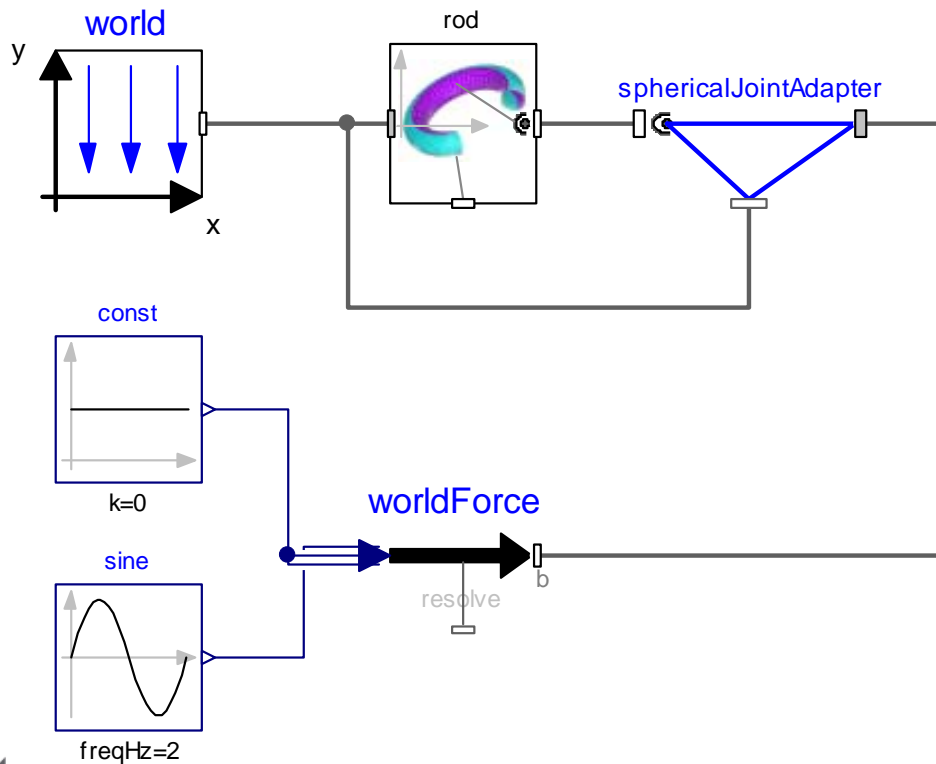
- Modelica Multibody Basics
- Exercise 1: Control of an inverse pendulum
- Modelica Multibody Advanced
- Exercise 2: Hexapod
- FlexibleBodies Library: Beams
- Exercise 3: Aircraft Fin
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- Exercise 4: Rod



Example 4: Rod

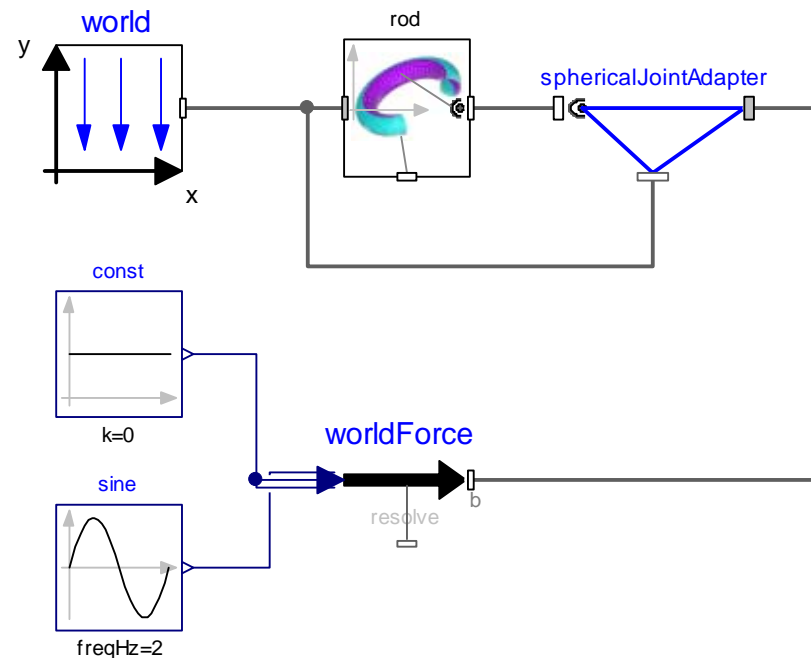
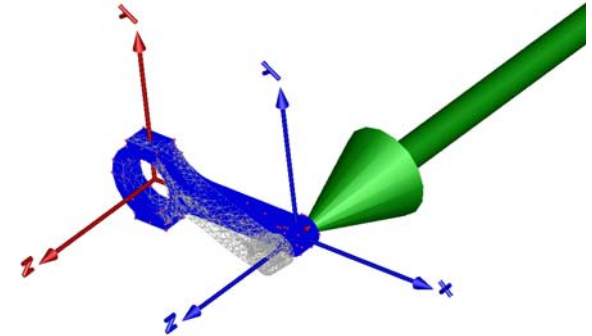
➤ 1st step:

- introduce world and ModalBody- model
- assign SID-file .../Extras/Data/rodV2.SID_FEM
- assign OBJ-file .../Extras/Data/rodV2small.obj



Example 4: Rod

- 2nd step: find node number to apply force
 - simulate trivial model from 1st step
 - zoom and pick node graphically
- 3rd step:
 - introduce node number
 - connect adapter
 - apply force



FlexibleBodies Library: Quo vadis?

- ModalBody: some tasks and goals
 - relies on an appropriate FE-preprocessor
 - a 3rd third party product
 - in principle agreements were made, but no contracts are yet signed
 - the 1st implementation uses additional c-code
 - there is no distribution process to support the application on real-time platforms today
 - the 2nd implementation in pure Modelica code in preparation
 - good enough for moderate large models
 - an additional license key called ExtFlexibleBodies
 - graphical nodes-picking requires improvements
- Besides beams: implementation of other generic structures „on demand“
 - brake discs: annular Kirchhoff plate
 - framework structures